BERARDO RUFFINI

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Personal Data and contacts

- Place of birth: Fiesole (Florence)
- Nationality: Italian
- e-mail: berardo.ruffini@unibo.it

Current Position. Associate professor, Dipartimento di Matematica dell'Università di Bologna

Previous position.

2019 – 2022 Assistant professor (RTD B) at the Dipartimento di Matematica di Bologna 2015 – 2019 Maître de Conférences at the Université de Montpellier 2 (permanent position).

Qualifications.

- February 2014 French qualification for the position of Maître de Conférences, Section 25 Mathématiques and 26 Mathématiques appliqués et applications des mathématiques.
- July 2018 Italian qualification for the position of Professore Associato (Abilitazione Scientifica Nazionale). Section 01/A3 Analisi Matematica, Probabilità e statistica matematica.
- July 2022 Italian qualification for the position of Professore Ordinario (Abilitazione Scientifica Nazionale). Section 01/A3 Analisi Matematica, Probabilità e statistica matematica.

Education and Formation

- January 2015– August 2015 Postdoc "Hadamard" at the Ecole Polytechnique (Palaiseau) under the supervision of A. Chambolle.
- January 2014–December 2015 Postdoc of the ANR project GEOMETRYA in Grenoble under the supervision of H. Pajot.
- November 2013 Perfezionamento at the Scuola Normale Superiore di Pisa (equivalent to the Ph.D. degrees), with the final degree 70/70 cum laude. Title of the thesis: *Optimization problems for solutions of elliptic equations and stability issues* Advisor: G. Buttazzo.
- April 2010. Master degree, magna cum laude, at the University of Florence. Title of the thesis: "Riduzione al caso radiale per una versione quantitativa della disuguaglianza di Gagliardo-Nirenberg" (Reduction to the radial case for a quantitative version of the Gagliardo-Nirenberg inequality). Advisor: F. Maggi

RESEARCH

My research interests are mainly in the areas of Calculus of Variations, Shape Optimization problems, Geometric Measure Theory, PDE, Optimal Transport Theory and non-local operators.

PAPERS

Publications on peer-reviewed international papers.

- (1) M. GOLDMAN, M. NOVAGA, B. RUFFINI. Rigidity of the ball for an isoperimetric problem with strong capacitary repulsion. **JEMS** accepted for publication.
- (2) C. B. MURATOV, M. NOVAGA, M., B. RUFFINI. Conducting Flat Drops in a Confining Potential Arch. Ration. Mech. Anal. 243 (2022), no. 3, 1773-1810.

- (3) M. GOLDMAN, M. NOVAGA, B. RUFFINI. Reifenberg flatness for quasi-minimizers of the perimeter under minimal assumptions Proc. Amer. Math. Soc. 150 (2022), no. 3, 1153–1165.
- (4) E. CINTI, R. OGNIBENE, B. RUFFINI, A quantitative stability inequality for fractional capacities. Math. Eng. 4 (2022), no. 5, Paper No. 044, 28 pp.
- (5) D. MAZZOLENI, B. RUFFINI A spectral shape optimization problem with a nonlocal competing term. Calc. Var. PDE 60 (2021), no. 3, Paper No. 114, 46 pp.
- (6) P. CASTILLON, B. RUFFINI A spectral characterization of geodesic balls in non-compact rank one symmetric spaces. Ann. Sc. Norm. Super. Pisa Cl. Sci. (5) 19 (2019), no. 4, 1359–1388.
- (7) M. GOLDMAN, M. NOVAGA, B. RUFFINI On minimizers of an isoperimetric problem with long-range interactions and convexity constraint. **Anal. PDE** 11 (2018), no. 5, 1113–1142.
- (8) C. MURATOV, M. NOVAGA, B. RUFFINI On equilibrium shapes of charged flat drops. Comm. Pure Appl. Math. 71 (2018), no. 6, 1049–1073.
- (9) L. BRASCO, G. FRANZINA, B. RUFFINI, Schrödinger operators with negative potentials and Lane-Emden densities. J. Funct. Anal. 274 (2018), no. 6, 1825–1863.
- (10) A. CHAMBOLLE, M. NOVAGA, B. RUFFINI, Some results on anisotropic fractional mean curvature flows. Interfaces Free Bound. 19 (2017), no. 3, 393–415.
- (11) J. AGHILI, D. A. DI PIETRO, AND B. RUFFINI A hp-Hybrid High-Order method for variable diffusion on general meshes. Comput. Methods Appl. Math. 17 (2017), no. 3, 359–376.
- (12) M. GOLDMAN, B. RUFFINI, M. Goldman, B. Ruffini, Equilibrium shapes of charged droplets and related problems: (mostly) a review. **Geom. Flows** 2 (2017), 94–104.
- (13) L. BRASCO, B. RUFFINI Compact Sobolev embeddings and torsion functions. Ann. Inst. H. Poincaré Anal. Non Linéaire 34 (2017), no. 4, 817–843.
- (14) M. GOLDMAN, M. NOVAGA, B. RUFFINI. Existence and stability for a non-local isoperimetric model of charged liquid drops. Arch. Ration. Mech. Anal. 217 (2015), no. 1, 1–36.
- (15) A. DI CASTRO, M. NOVAGA, B. RUFFINI, E. VALDINOCI. Non-Local Isoperimetric Problems. Calc. Var. Partial Differential Equations 54 (2015), no. 3, 2421–2464.
- (16) M. MARINI, B. RUFFINI, On a class of weighted Gauss-type isoperimetric inequalities and applications to symmetrization. **Rend. Semin. Mat. Univ. Padova** 133 (2015), 197–214.
- (17) G. BUTTAZZO, A. GEROLIN, B. RUFFINI, B. VELICHKOV, Spectral Optimization Problems for Schrödinger Operators, J. Éc. polytech. Mat., 1 (2014), p. 71–100.
- (18) B. RUFFINI, Stability Theorems for Gagliardo-Nirenberg-Sobolev inequalities. Rev. Mat. Complut. 27 (2014), no. 2, 509–539.
- (19) M. NOVAGA, B. RUFFINI, Brunn-Minkowski inequality for the 1-Riesz capacity and level set convexity for the 1/2-Laplacian. J. Convex Anal. 22 (2015), no. 4, 1125–1134.
- (20) C. DE LELLIS, M. FOCARDI, B. RUFFINI, A note on the Hausdorff dimension on the singular set for minimizers of the Mumford-Shah Energy. Adv. Calc. Var. 7 (2014), no. 4, 539–545.

- (21) G. BUTTAZZO, B. RUFFINI, B. VELICHKOV, Shape Optimization Problems for Metric Graphs. ESAIM Control Optim. Calc. Var. 20 (2014), no. 1, 1–22.
- (22) L. BRASCO, G. DE PHILIPPIS, B. RUFFINI, Spectral optimization for the Stekloff-Laplacian: the stability issue, **J. Funct. Anal.** 262 (11), (2012), 4675–4710.

Proceedings

 B. RUFFINI Optimization problems with non-local repulsion Bruno Pini Math. Anal. Semin., 12(1) Università di Bologna, Alma Mater Studiorum, Bologna, 2022, 101–121.

Some Talks

- Spectral stability for the Stekloff-Laplacian and for a class of weighted perimeters, XXII Convegno Nazionale di Calcolo delle Variazioni. Levico, February 2012.
- Shape optimization problems for graphs Seminario di Analisi Dipartimento di Matematica "L. Tonelli". Pisa, May 2012.
- Stability of optimal shapes for the Stekloff-Laplacian Seminario di Analisi, Dipartimento di Matematica "U. Dini", Firenze, March 2012.
- Spectral Optimization for the Laplacian with Robin Boundary condition. Seminario informale di analisi delle Classi di Perfezionamento della Scuola Normale Superiore. October 2012.
- Optimal potentials for Schrödinger operators. Ph.D. research Seminar, Dipartimento di Matematica. "U. Dini", Firenze, March 2013.
- Optimization of Schrödinger operators. Analysis Research Seminar, Erlangen, March 2013.
- Two short talks during the thematic sessions on *Shape optimization problems* and on *Optimal transportation and applications* during a summer school in Benasque in August 2013.
- Variational problems with non-local energies. Séminaire de l'équipe EDP-MOISE, Grenoble, January 2014.
- *Problemi variazionali non locali*. XXIV Convegno Nazionale di Calcolo delle Variazioni. Levico, January 2014.
- Stabilité pour problèmes isopérimètriques avec poids et applications. Rencontres de l'ANR, Orsay (Paris), Mars 2014.
- Optimal Potentials for Schrödinger Operators. GB60 (A workshop in honor of the 60th birthday of Giuseppe Buttazzo), Pise, May 2014.
- A non-local variational model of charged liquid drops, Séminaire d'analyse appliquée de l'I2M, Marseille, June 2014.
- Isoperimetric problems with non-local penalization terms, Isoperimetric Problems Between Analysis and Geometry, Pise, June 2014.
- Non-Local isoperimetric problems, Seminario di Analisi, Dipartimento di Matematica "U. Dini", Firenze, October 2014.
- On some non-local isoperimetric problems, Séminaire du groupe de Travaille CalVa, Paris, March 2015.
- Non-local isoperimetric problems, Seminario di Analisi Dipartimento di Matematica "L. Tonelli". Pisa, June 2015.
- Inégalités isopérimètriques, inégalités fonctionnelles et trou spectral, Séminaire du groupe DAR-BOUX, Montpellier, September 2015.
- Sur un modèle isopérimétrique d'une goutte liquide chargée. Séminaire du groupe ACSIOM, Montpellier, October 2015.
- On fractional isoperimetric problems One-day conference on Calculus of Variations, Lille, October 2015.

- Compact Sobolev embedding and torsion function , Geometric aspects of PDE's and functional inequalities, Cortona, May 2016.
- A variational model for charged liquid drops, short talk at PICOF, Autrans, June 2016.
- Compact Sobolev embedding and torsion function, Séminarire commune d'Analyse Géometrique, Luminy, September 2016.
- On a variation model for charged liquid drops, "GMT, Shape Optimizations and Free Boundaries". SISSA, Trieste, october 2016.
- Compact Sobolev embedding and torsion function, XXVII Convegno Nazionale di Calcolo delle Variazioni. Levico, February 2017.
- Some results on a variational model for the equilibria of a charged liquid drop. Séminaire du laboratoire J. Coulombe, departement de Physique. Montpellier, February 2017.
- On the consistency of a BMO-type scheme and convexity preservation for a fractional mean curvature flow. Curves and networks in geometric analysis, Pise, June 2017.
- Some results on an isoperimetric model for charged liquid drops. Seminario di Analisi Matematica, Ferrara, February 2018.
- Some results on an isoperimetric model for charged liquid drops Seminario di Analisi, Dipartimento di Matematica "U. Dini", Firenze, March 2018.
- Some results on a isoperimetric model for charged drops Workshop in Calculus of Variations at Paris Diderot, June 2018.
- The Brock-Weinstock inequality on harmonic manifolds, séminaire commun d'analyse géometrique. Luminy, September 2018.
- Some results on an isoperimetric model for charged liquid drops, Bologna, November 2018.
- Sobolev immersions and Torsion functions Variational and pde problems in geometric analysis, II. Bologna, May 2019.
- Charged drops, a variational model part II. Short communication at Convegno nazionale UMI. Pavia, September 2019.
- An isoperimetric problem for charged liquid drops, Mynisimposium for the short conference: Recent developments in nonlocal geometric variational problems. ICIAM 2019, Valencia. July 2019
- *Perimeter vs Capacity* Winter School on Reaction Diffusion PDE's and Optimization, Dipartimento di Matematica e Fisica, Univ. Cattolica di Brescia. January 2020
- Optimal design problems with repulsive term Seminario Pini, Dipartimento di Matematica di Bologna. May 2021
- Non-local isoperimetric problems, Isoperimetric problems, Pisa, June 2022
- News about an isoperimetric problem with strong capacitary repulsion Anisotropic isoperimetric problems & related topics, Rome, September 2022
- Spectral energies with repulsion Seminario Pini, Dipartimento di Matematica di Bologna. June 2023
- Dimensional estimates in a branched transport model for type-I superconductors Calculus of Variations in Siena, February 2024.
- From energy bounds to dimensional estimates in a branched transport model for type-I superconductors CalVaFer - Calculus of Variations in Ferrara, March 2024
- Shape optimization for Hartree energies Calculus of Variations and Free Boundary Problems VIII, April 2024
- An open problem around the Kohler-Jobin inequality 50 Anni di Calcolo delle Variazioni, May 2024

Some visits

• University of Pavia, Pavia. Invited by Prof. Aldo Pratelli, September 2012

- Department Matematik, Erlangen. Invited by Prof. Aldo Pratelli, March 2013
- Max Planck Institut, Leipzig. Invited by Dr. Michael Goldman, April 2013
- University of Florence, Florence. Invited by Dr. Chiara Bianchini, October 2014.
- University of Pise, Pise. Invited by Prof. Matteo Novaga, February 2015.
- Université de Paris 7, Paris. Invited by M. Goldman, CNRS. July 2016.
- SISSA, Trieste. Invited by Prof. G. De Philippis. June 2017.
- NJIT, New York. Invited by Prof. C. Muratov. May 2018.
- University of Florence, Florence. Invited by Prof. C. Bianchini. June 2018.
- Università di Pisa, Pisa. Invited by Prof. M. Novaga. February 2022.
- Paris 7, Paris. Invited for 3 weeks by Prof. M. Goldman via a MOVEON program. Mars 2022.
- Paris, Ecole Polytechnique, Paris. Invited for 2 weeks by Prof. M. Goldman. Mars 2023.
- Rome, Sapienza, invited by M. Ponsiglione. June 2023.

Committee member for the Ph.D. defense

2023 Angelo Ninno (Roma, Sapienza).

2023 Paolo De Donato (Roma, Sapienza).

TEACHING

I performed some exercices classes during my Ph.D in Pise, and my first postdoc in Grenoble. Since September 2015 I taught about 190 hours per year at the University of Montpellier at every undergraduate level. Since September 2019 I taught 90 hours per year first at the first academic year of Ingegneria, Bologna. Details are given below.

- 2012-Teaching assistant for the course (given by Prof. L. De Pascale) "Analisi Matematica 1" (Calculus 1), Faculty of Engineering, University of Pisa (25 hours).
- 2013-Teaching assistant for the course (given by Prof. M. Novaga) "Analisi Matematica 1" (Calculus 1), Faculty of Engineering, University of Pisa (25 hours).
- 2014 (september-december) Lectures in "Mathematics for the Biology", University of Grenoble (30 hours).
- 2015 (september-december) Exercice classes in "Mathematics for the Biology", University of Montpellier (32 hours).
- 2015 (september-december) Exercice classes in Algebre and Analysis I. University of Montpellier (48 hours).
- 2015 (september-december) Exercice classes in Analysis 3, University of Montpellier (39 hours).
- 2016 (september-december) Exercice classes in "Mathematics for the Biology", University of Montpellier (32 hours).
- 2016 (september-december) Exercice classes in Algebre and Analysis I. University of Montpellier (48 hours).
- 2016 (september-december) Exercice classes in Analysis 3, University of Montpellier (39 hours).
- 2016 (september-december) Lectures for a Master 1 course in Functional analysis (Master 1). University of Montpellier (30 hours).
- 2017 (january) Lectures for Master 2 and Ph.D. students on Gamma-convergence theory, University of Montpellier (14 hours).
- 2017 (september-december) Exercice classes in "Mathematics for the Biology", University of Montpellier (32 hours).
- 2017 (september-december) Exercice classes in Algebre and Analysis I, University of Montpellier (48 hours).
- 2017 (september-december) Lectures (and exercices classes) for the second year undergraduate course in Analysis 3, University of Montpellier (36+39 hours).
- 2017 (september-december) Lectures for a Master 2 course on Elliptic PDE (24 hours).

- 2018 (september-december) Exercice classes in "Mathematics for the Biology", University of Montpellier (32 hours).
- 2018 (september-december) Exercice classes in Algebre and Analysis I, University of Montpellier (48 hours).
- 2018 (september-december) Lectures (and exercices classes) for the second year undergraduate course in Analysis 3, University of Montpellier (36+39 hours).
- 2018 (september-december) Lectures for a Master 2 course on Elliptic PDE (24 hours).
- 2019-2023 (september-december) Courses on Analisi Matematica I, Ingegneria Chimica e Biochimica, Università di Bologna.
- 2022-2023 Course on Calculus of Variations (24h).
- 2023 Courses on Analisi Matematica, Fisica, Università di Bologna.

1. TUTORIAL AND ORGANIZING ACTIVITY

- Advisor of the Magistrale thesis of Lucia Rota Bulò. "Around optimal transport". 2024
- Co-organiser of the conference NON-pub23, Bologna, June 2023.
- Co-organiser of the conference "Shape Optimization, related topics and applications", Roskoff, June 2022
- Co-organiser of the conference "Variational methods and applications", Centro De Giorgi, Pisa, September 2021.
- Co-organiser of the conference "Rencontre ANR". Montpellier, June 2019.
- Co-organiser of a meeting conference between the Montpellier and the Toulouse Mathematical labs. April 2019.
- Organizer of the seminars of analysis and PDE at the IMAG, Université de Montpellier
- Advisor of the Master 2 Thesis of Mohamad Webbe. Argument: "Optimal constants for the quantitative Sobolev inequality".
- Member of the jury of 2 sessions of Master 2-thesis (Juin 2018, September 2018).

PARTICIPATION IN RESEARCH PROJECTS AND GRANTS

- PI of the project GNAMPA PACE CUP-E55F22000270001, grant of 4500 euros.
- Member at the 65% and local coordinator of the three-years French ANR project SHAPO ANR-18-CE40-0013 (Grant of approximately 480k euros, 2018-2021). Principal investigator: J. Lamboley.
- Winner of a PEDR (Prime d'Encadrement Doctoral et de Recherche) with an annual grant of 5000 euros per year (for the 4-years 2017-2021).
- Winner of three (consecutive) grants PEPS-Jeunes chercheurs, with M. Goldman with a research grant of 6000 euros, in the years 2016, 2017 and 2018.

Reviewing

Referee for "Annales Academiae Scientiarum Fennicae", "Nonlinear Analysis Series A: Theory, Methods & Applications", "Applicable Analysis", "JMAA", "Geometric Flows", "COCV", "Trans. AMS", "Calc. Var. & PDE", "JMAA", "CPAA", "Ann. Global An. and Geom.". Reviewer on Mathscinet.

LANGUAGE SKILLS

- Italian, native
- English, fluent
- French, fluent

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